AweSums

Marvels and Mysteries of Mathematics • LECTURE 1

Peter Lynch School of Mathematics & Statistics University College Dublin

Evening Course, UCD, Autumn 2020



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Outline

Introduction

- **Overview**
- **Beautiful Spirals**
- The Golden Ratio
- Symmetry
- **Recreational Mathematics**
- Visual Maths 1

Distraction 1: A Piem



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Aim of the Course

AweSums

The course will run over six (6) lectures, from 5 October to 16 November.

No lecture on 26th October. So, the course splits into 3 + 3.

The aim of the course is to show you

- The great beauty of mathematics;
- Its tremendous utility in our daily lives;
- The fun we can have studying maths.



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Meaning and Content of Mathematics

The word Mathematics comes from Greek $\mu\alpha\theta\eta\mu\alpha$ (máthéma), meaning "knowledge" or "study" or "learning".

It is the study of topics such as

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- Quantity
- Structure
- Space

Overview

Change



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Meaning and Content of Mathematics

The word Mathematics comes from Greek $\mu\alpha\theta\eta\mu\alpha$ (máthéma), meaning "knowledge" or "study" or "learning".

It is the study of topics such as

- Quantity: [Numbers. Arithmetic]
- Structure: [Patterns. Algebra]
- Space: [Geometry. Topology]
- Change: [Analysis. Calculus]



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Tom Lehrer: Mathematician, Musician and Comic Genius

ThatsMaths article in *The Irish Times* in September 2018 about mathematician and comic genius Tom Lehrer. (You can find articles using the Search Box.)

https://thatsmaths.com/

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https://thatsmaths.com/

- /Users/peter/Dropbox/Music/Videos.html
- Run Video (vsn 1)
- List Keywords
- Run Video (vsn 2) later.



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Notes and Slides

 All the slides will be available online: http://mathsci.ucd.ie/~plynch/AweSums [just Google for "Peter Lynch UCD"]

- No notes are to be provided.
 Why Not? See next slide.
- Additional Reading Recommendations.
- Optional Exercises and Problems.

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 Why Not? See next slide.
- Additional Reading Recommendations.
- Optional Exercises and Problems.
- No Assignments!
- No Assessments!
- No Examinations!

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Why No Notes?

- Maths is NOT a Spectator Sport
- Active engagement is essential to understanding.
- You should take your own notes:

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- This involves repetition of what you hear.
- This involves repetition of what you see.
- What you write passes through your mind!

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This process is a great help to memory.



Intro

Lectures

- Classes run from 7pm to 9pm.
- 120 minutes intensive lecturing too long (both for you and for me).
- Educational Theory:

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Attention & retention both decrease with time.

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Class will be broken into short sections.

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Intro

Lectures

- Classes run from 7pm to 9pm.
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 - Attention & retention both decrease with time.

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Class will be broken into short sections.

If you cannot attend a class:

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- Please do not bother to email me.
- There is no need to give any reasons.

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The presentation slides will be available.



Intro

Communications

In the unlikely event that a class has to be cancelled,

- I will notify "Adult & Lifelong Learning".
- You may wish to form a WhatsApp group.

I will also tell you about other mathematical events in Dublin if I hear about them.



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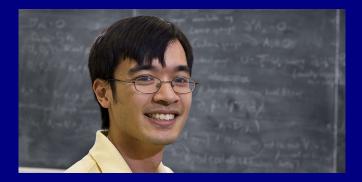
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Hamilton Lecture, 2020



The Cosmic Distance Ladder Friday, October 16, 16:00 Free online event: booking essential www.ria.ie



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"Typical" Structure of a Class

- 1. Problem: Background and Theory
- 2. Distraction (10 min)
- 3. Some History of the problem
- 4. Another Distraction
- 5. Exercises, Puzzles, History
- 6. Questions & Discussion

Total duration: about 120 minutes.



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"Typical" Structure of a Class

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- 6. Questions & Discussion

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Total duration: about 120 minutes.

I will (normally) be available after classes to answer questions or offer clarifications.

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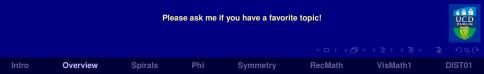
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Some Distractions

- Visual Awareness: Maths Everywhere
- Puzzles: E.g. Watermelon Puzzle
- Sieve of Eratosthenes
- The Greek Alphabet
- Lateral Thinking in Maths
- Lecture sans paroles
- How Cubic and Quartic Equations were cracked
- Four-colour Theorem
- Online Encyclopedia of Integer Sequences



I expect a group with a wide range of knowledge and "mathematical maturity".

Everybody should benefit from the course.

If anything is unclear, SHOUT OUT! or whisper!

If something is missing, let me know.

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Feedback on the course is very welcome.

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Intro

Classes begin at 7 pm. and run till 9 pm.



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Classes begin at 7 pm. and run till 9 pm.

There seem to be two options:

- Break at 7:50 for 10, 15 or 20 minutes.
- Don't break at all !!!

I have no strong views but I suspect that there might be a riot if we do not have a break.



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Classes begin at 7 pm. and run till 9 pm.

There seem to be two options:

- Break at 7:50 for 10, 15 or 20 minutes.
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I have no strong views but I suspect that there might be a riot if we do not have a break.

Let's have a poll: Who wants a break?



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Popular Mathematics Books

- 1. John H Conway and Richard K Guy, 1996: *The Book of Numbers.* Copernicus, New York.
- 2. ♡ ⇒ John Darbyshire, 2004: *Prime Obsession.* Plume Publishing.
- ♡ ⇒ William Dunham, 1991: Journey through Genius. Penguin Books.
- 4. Marcus Du Sautoy, 2004: *The Music of the Primes.* Harper Perennial.
- 5. ♡ ⇒ Richard Elwes, 2010: *Mathematics 1001.* Firefly Books.
- 6. Peter Lynch, 2016: *That's Maths.* Gill Books. Published in October 2016.



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A Splendid Spiral in Booterstown



This sandbank, a beautiful spiral form, has slowly built up on the beach near Booterstown Station.

Spirals are found throughout the natural world.



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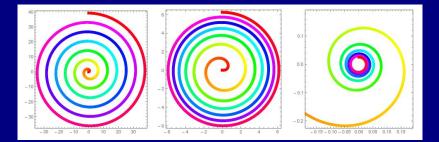
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Some Mathematical Spirals



Archimedes Spiral. Fermat Spiral. Hyperbolic Spiral.



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The Nautilus Shell: a logarithmic Spiral.





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The Sunflower: Groups of Spirals



Spirals in the Physical World



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Spirals in the Physical World



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https://thatsmaths.com/



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Fibonacci Numbers

- Count the petals on a flower.
- Count leaves on a stem or bumps on an asparagus.
- Look at patterns on pineapples/pine-cones.
- Study the geometry of seeds on sunflowers.



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Fibonacci Numbers

- Count the petals on a flower.
- Count leaves on a stem or bumps on an asparagus.
- Look at patterns on pineapples/pine-cones.
- Study the geometry of seeds on sunflowers.

In all cases, we find numbers in the sequence:

1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, ...

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This is the famous Fibonacci sequence.

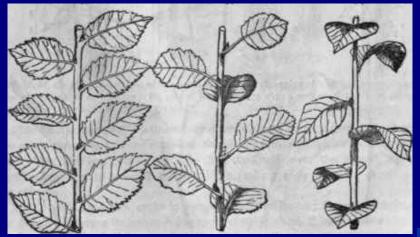
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Fibonacci and Phyllotaxis





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Vi Hart's Videos

There are several mathematical videos on YouTube presented by Vi Hart.

Some of the ones on Fibonacci Numbers are at:

https://www.youtube.com/
watch?v=ahXIMUkSXX0

It is *much easier* to go to Youtube and search for "Vi Hart Fibonacci"



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"Vi Hart Fibonacci"

Let's take a peek!

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Golden Ratio and Fibonacci Numbers

The Golden Ratio is a number defined as

$$\phi = \frac{1 + \sqrt{5}}{2} \approx 1.618$$

It is intimately connected with the Fibonacci Numbers.



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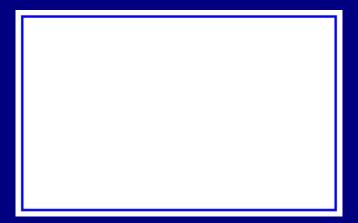
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Golden Rectangle



Ratio of breath to height is $\phi = \frac{1+\sqrt{5}}{2} \approx 1.6$.



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Golden Rectangle in Your Pocket



Aspect ratio is about $\phi = \frac{1+\sqrt{5}}{2} \approx 1.618$.



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The Fibonacci sequence is the sequence

 $\{0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, \dots\}$

where each number is the sum of the previous two.



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The Fibonacci sequence is the sequence $\{0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, \dots\}$ where each number is the sum of the previous two. The Fibonacci numbers obey a recurrence relation

$$F_{n+1}=F_n+F_{n-1}$$

with the starting values $F_0 = 0$ and $F_1 = 1$.



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Intro

The Fibonacci sequence is the sequence $\{0,1,1,2,3,5,8,13,21,34,55,89,144,\dots\}$ where each number is the sum of the previous two. The Fibonacci numbers obey a recurrence relation

$$F_{n+1}=F_n+F_{n-1}$$

with the starting values $F_0 = 0$ and $F_1 = 1$.

The explicit expression for the Fibonacci numbers is

$$F_{n} = \frac{1}{\sqrt{5}} \left[\frac{1+\sqrt{5}}{2} \right]^{n} - \frac{1}{\sqrt{5}} \left[\frac{1-\sqrt{5}}{2} \right]^{n}$$
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Let's consider the sequence of ratios of terms $\frac{1}{1}, \frac{2}{1}, \frac{3}{2}, \frac{5}{3}, \frac{8}{5}, \frac{13}{8}, \frac{21}{13}, \frac{34}{21}, \dots$



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Let's consider the sequence of ratios of terms

$$\frac{1}{1}, \ \frac{2}{1}, \ \frac{3}{2}, \ \frac{5}{3}, \ \frac{8}{5}, \ \frac{13}{8}, \ \frac{21}{13}, \ \frac{34}{21}, \ \dots$$

The ratios get closer and closer to the golden number:

$$rac{F_{n+1}}{F_n} o \phi$$
 as $n o \infty$

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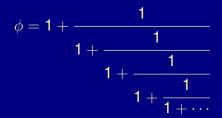
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Exotic Expressions for ϕ

We can write ϕ as a continued fraction





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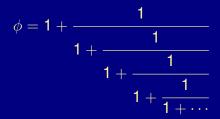
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Exotic Expressions for ϕ

We can write ϕ as a continued fraction



We can also write it as a continued root

$$\phi = \sqrt{1 + \sqrt{1 + \sqrt{1 + \sqrt{1 + \cdots}}}}$$



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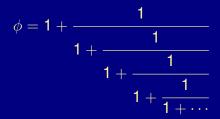
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Exotic Expressions for ϕ

We can write ϕ as a continued fraction



We can also write it as a continued root

$$\phi = \sqrt{1 + \sqrt{1 + \sqrt{1 + \sqrt{1 + \cdots}}}}$$

These extraordinary expressions are actually quite easy to demonstrate!



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Fibonacci Numbers in Nature

Look at post Sunflowers and Fibonacci: Models of Efficiency on the *ThatsMaths* blog:

thatsmaths.com



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Ubiquity and Beauty of Symmetry

Symmetry is all around us.

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- Many buildings are symmetric.
- Our bodies have bilateral symmetry.
- Crystals have great symmetry.
- Viruses can display stunning symmetries.
- At the sub-atomic scale, symmetry reigns.
- Galaxies have many symmetries.

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The Taj Mahal





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A Face with Symmetry: Halle Berry





Berry Halle



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An Asymmetric Face: You know Who!





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Symmetry and Group Theory

Symmetry is an essentially geometric concept.

The mathematical theory of symmetry is algebraic.

The key concept is that of a group.



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Symmetry and Group Theory

Symmetry is an essentially geometric concept.

- The mathematical theory of symmetry is algebraic.
- The key concept is that of a group.

A group is a set of elements such that any two elements can be combined to produce another.

Instead of giving the mathematical definition, I will give an example to make things clear.



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The *Dihedral Group* D₁

The group of symmetries of the human face and of all biological forms with bilateral symmetry. We could call D_1 the *Janus Group*.

- I: The Identity transformation
- **R**: Reflection about central line

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Table : First Dihedral Group D₁.



This is how we combine, or multiply transformations.

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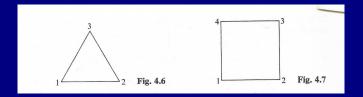
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From 2 to 3 Dimensional Symmetry



Tetrahedron	Cube	Octahedron	Dodecahedron	Icosahedron	
Four faces	Six faces	Eight faces	Twelve faces	Twenty faces	
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Recreational Mathematics

Recreational mathematics puts the focus on insight, imagination and beauty.

Recreational Maths includes the study of

- The culture of mathematics,
- Its relevance to art, music and literature,
- Its role in technology,
- Mathematical games and puzzles,
- The lives of the great mathematicians.



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Many Resources Available

Great variety of books on popular mathematics.

Wealth of literature suitable for a general audience

Magazines available free online.

One of the best is the e-zine Plus:

https://plus.maths.org/.

All past content is available and is a valuable resource for school students and teachers.



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Content of an Earlier Course

Lecture	Content
1	Outline of Course. Emergence of Numbers.
2	Georg Cantor. Set Theory.
3	Pythagoras. Irrational Numbers.
4	Hilbert. Gauss. The Real Number Line
5	Powers. Logarithms. Prime Numbers.
6	Functions. Archimedes. Natural Logs.
7	Exponential Growth. Euler. Sequences & Series.
8	Trigonometry. Taylor Series.
9	Basel Problem. Complex Numbers. Euler's Formula.
10	Prime Number Theorem. Riemann Hypothesis.

This year's course will be different: Better!



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Visual Maths 1



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To Begin: An Optical Illusion

- A cautionary tale:
- In maths we often use pictures to prove things.
- This is usually very helpful.
- However, it can sometimes mislead us.
- Let us look at the Fraser Spiral.



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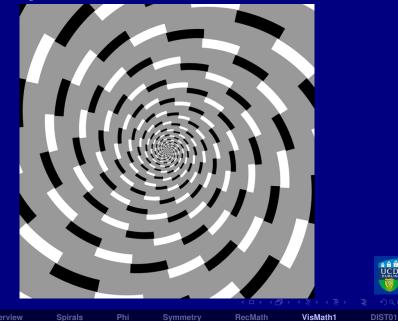
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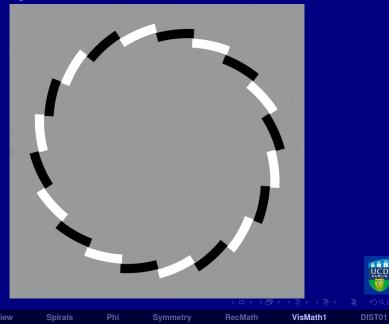
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Fraser Spiral



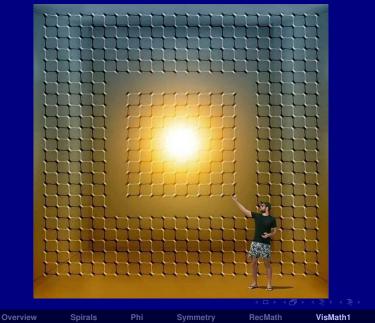
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Fraser Spiral



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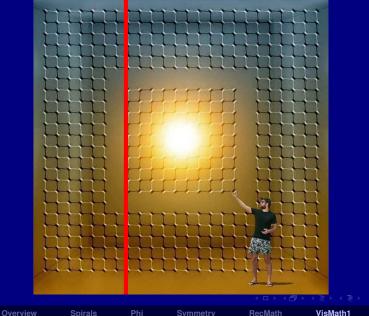


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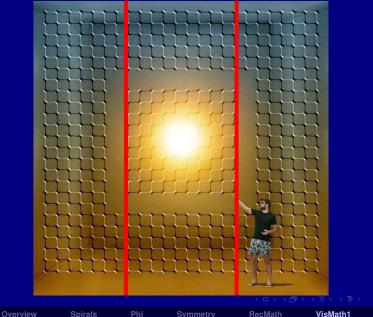
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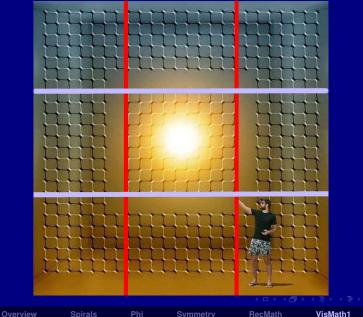


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Visual Maths Proofs

Can the sum of an infinite number of quantities have a finite value?

Let's look at the infinite series

$$S = \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \cdots$$



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Visual Maths Proofs

Can the sum of an infinite number of quantities have a finite value?

Let's look at the infinite series

$$S = \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \cdots$$

Each term is half the size of the preceding one.

The terms are getting smaller but it is not obvious that the series converges.



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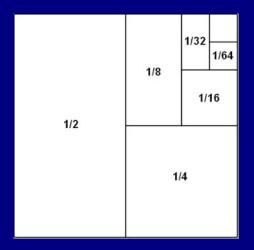
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A picture makes everything clear:



Unit Square: At each stage, we add half the remainder of the square.



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Conclusion

The infinite series

$$S = \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \cdots$$

has a finite sum:

$$\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots = 1$$

The terms are getting smaller quickly enough for the series to be convergent.



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Another Simple Proof

What is the sum of the first n odd numbers?

$$1 = 1^2$$
 $(1+3) = 4 = 2^2$ $(1+3+5) = 9 = 3^2$

Is this pattern continued? Can we prove it?



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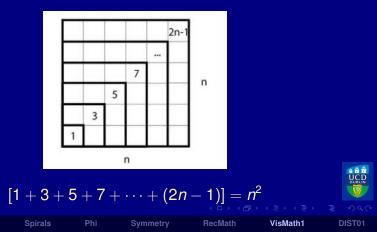
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Another Simple Proof

What is the sum of the first *n* odd numbers?

$$1 = 1^2$$
 $(1+3) = 4 = 2^2$ $(1+3+5) = 9 = 3^2$

Is this pattern continued? Can we prove it?



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What is the sum of the first *n* even numbers?

$$S = 2 + 4 + 6 + 8 + \cdots 2n$$



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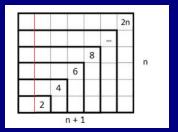
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What is the sum of the first *n* even numbers?

 $S = 2 + 4 + 6 + 8 + \cdots 2n$



We just add a column on the left. This increases each term of the sequence of odd numbers by 1.

$$[2+4+6+\cdots+2n] = n(n+1)$$



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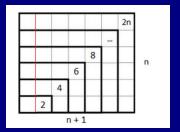
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What is the sum of the first *n* even numbers?

$$S = 2 + 4 + 6 + 8 + \cdots 2n$$



We just add a column on the left. This increases each term of the sequence of odd numbers by 1.

$$[2+4+6+\cdots+2n] = n(n+1)$$

Now divide both sides by 2 to get:

$$[1+2+3+\cdots+n] = \frac{1}{2}n(n+1)$$



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Symmetry

RecMath

VisMath1

Outline

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- **Overview**
- **Beautiful Spirals**
- The Golden Ratio
- Symmetry
- **Recreational Mathematics**
- Visual Maths 1

Distraction 1: A Piem



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The ratio of circumference of circle to diameter is π .



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The ratio of circumference of circle to diameter is π . To 15-figure accuracy, π is equal to 3.14159265358979

How can we remember this without much effort?



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The ratio of circumference of circle to diameter is π . To 15-figure accuracy, π is equal to 3.14159265358979

How can we remember this without much effort?

Just remember this:

How I want a drink, Alcoholic of course,



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The ratio of circumference of circle to diameter is π . To 15-figure accuracy, π is equal to 3.14159265358979

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Just remember this:

How I want a drink, Alcoholic of course, After the heavy lectures involving quantum mechanics.



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How I want a drink, Lemonsoda of course, After the heavy lectures involving quantum mechanics.



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How I want a drink, Lemonsoda of course, After the heavy lectures involving quantum mechanics.

How I want a drink, Sugarfree of course, After the heavy lectures involving quantum mechanics.

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Repeat: To Remember π

To 15-figure accuracy, π is equal to

3.14159265358979

How can we remember this without much effort?

Just remember this:

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The reciprocal of π is approximately 0.318310 Can I remember the reciprocal?



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The reciprocal of π is approximately 0.318310 Can I remember the reciprocal?

How I remember the reciprocal!



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The reciprocal of π is approximately 0.318310 Can I remember the reciprocal?

How I remember the reciprocal! 3 1 8 3 10



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The reciprocal of π is approximately 0.318310 Can I remember the reciprocal?

How I remember the reciprocal! 3 1 8 3 10

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Now you know π and $1/\pi$ to an accuracy greater than you are ever likely to need!

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Thank you



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